

GITISA – Summer School 2012
Tecnologie sostenibili per la tutela dell'ambiente

LAGRANGIAN PARTICLE MODELS FOR AIRBORNE POLLUTANT DISPERSION

Applications and research purposes

DIIAR
Technical School of Milan
25/06/2012

Eng. Marco M. Zaccanti
University of Modena e Reggio Emilia
marcomichele.zaccanti@unimore.it

Abstract

- Air Quality Models: a brief introduction.
- Overview of a LPDM (SPRAY by Arianet S.r.l.).
- Case study: application of the model to an existing power plant.
 - Future research purposes.

Air Quality Models

- Atmospheric dispersion and chemical reactions of air pollutants.
- Space – time evolution of concentration field $\mathbf{C} = \mathbf{C}(x,y,z,t)$.

EMISSION SOURCES:

- *Industrial or power plants.*
- *Veichular traffic.*
- *Accidental chemical releases.*



Simulation of dispersion process

EULERIAN approach:

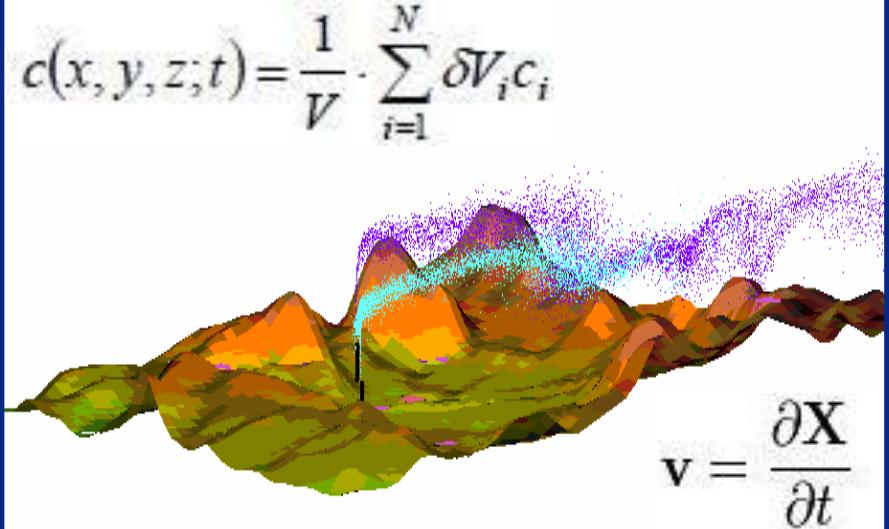
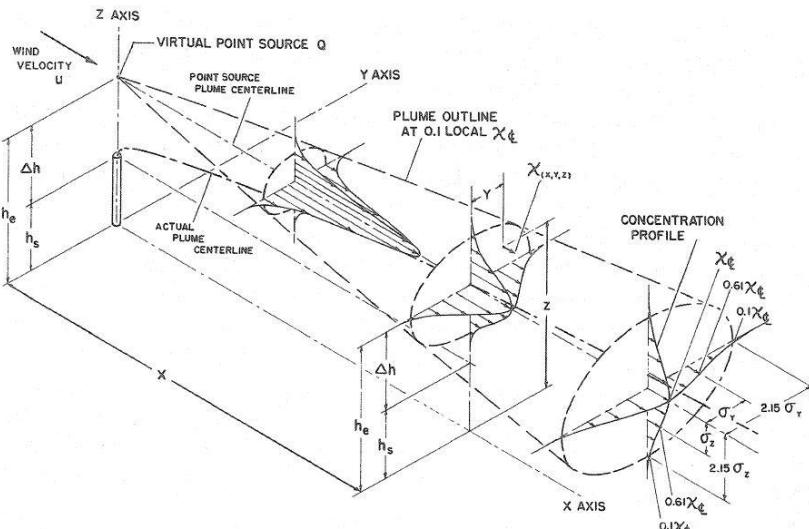
computing the $\mathbf{C} = \mathbf{C}(x,y,z,t)$
function as a solution of
General Diffusion Equation.

Gaussian solution (Sutton, 1969).

LAGRANGIAN approach:

discretizing the pollutant's emission
by a swarm of little particles
following the atmospheric flow.

Particle position equation



Input - output data for AQMs

EMISSION DATA

- Source: stack height and section.
- Pollutants: Temperature, exit speed, emission ratio.

METEOROLOGY

- Wind speed and temperature field.
- Turbulence scale parameters.

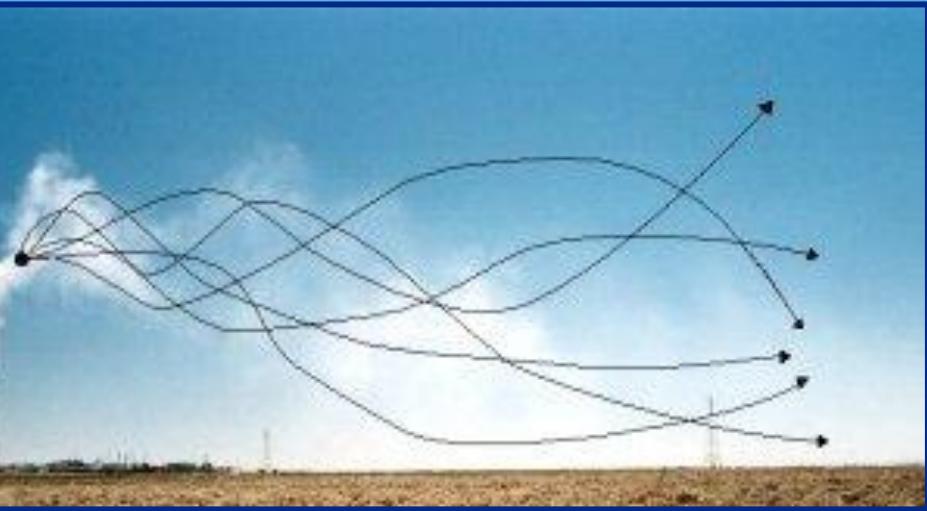
DOMAIN

- Topography and land use data.
- Computational spatial – time grid.

Air Quality Models

OUTPUT
Concentration field.

Lagrangian particle models (1)



$$u(t) = \bar{u} + u'(t)$$

$$v(t) = \bar{v} + v'(t)$$

$$w(t) = \bar{w} + w'(t)$$

Mean wind velocity

(meteo dataset)

Velocity fluctuation

(turbulent flows)

$$x(t + \Delta t) = x(t) + [\bar{u} + u'(t)] \Delta t$$

$$y(t + \Delta t) = y(t) + [\bar{v} + v'(t)] \Delta t$$

$$z(t + \Delta t) = z(t) + [\bar{w} + w'(t)] \Delta t$$

Lagrangian particle models (2)

Computing velocity fluctuations:

Langevin equation

$$\frac{du'}{dt} = -\frac{1}{T_{Lu'}} u'(t) + \eta(t) \quad (\eta \text{ independent from } u')$$

Thus, discretizing:

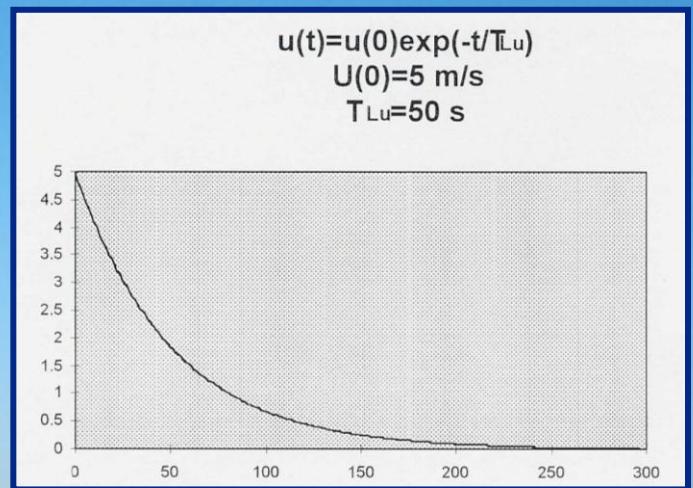
$$u'(t + \Delta t) = u'(t) - \frac{u'(t)}{T_{Lu'}} \Delta t + \eta \Delta t = \left(1 - \frac{\Delta t}{T_{Lu'}}\right) u'(t) + u''(t)$$

Defining: $r = e^{-\frac{\Delta t}{T_{Lu'}}} \approx 1 - \frac{\Delta t}{T_{Lu'}} \quad (\Delta t \ll T_{Lu'})$

$$u'(t + \Delta t) = r u'(t) + u''(t)$$

~~$$\overline{u'^2(t + \Delta t)} = r^2 \overline{u'^2(t)} + \overline{u''^2} + 2r \overline{u'(t) u''}$$~~

then, $\sigma_{u''} = \sigma_{u'} \sqrt{1 - r^2}$



Lagrangian particle models (3)

$$u'(t + \Delta t) = r_u u'(t) + u''(t + \Delta t) \sigma_{u'} \sqrt{1 - r_u^2}$$

$$v'(t + \Delta t) = r_v v'(t) + v''(t + \Delta t) \sigma_{v'} \sqrt{1 - r_v^2}$$

$$w'(t + \Delta t) = r_w w'(t) + w''(t + \Delta t) \sigma_{w'} \sqrt{1 - r_w^2}$$

$$r_i = e^{-\frac{\Delta t}{T_{Li}}} \quad \text{and } i = u, v, w$$

u'', v'', w'' random terms
from a *Wiener process*
(mean = 0, $\sigma = 1$)

Gaussian turbulence model for homogeneous and steady-state conditions.

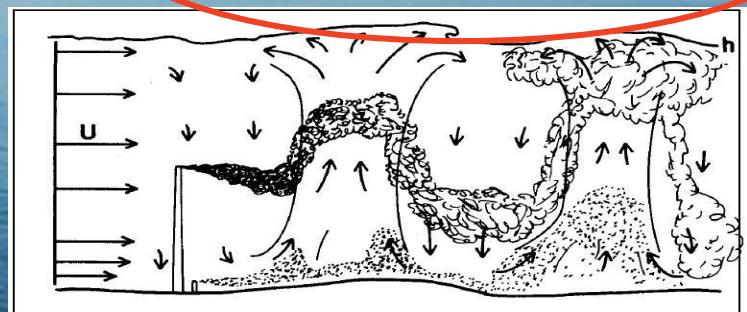
More complex schemes for inhomogeneous and NON – Gaussian turbulence

Fokker – Plank equation for PDF

Well – mixed criterion

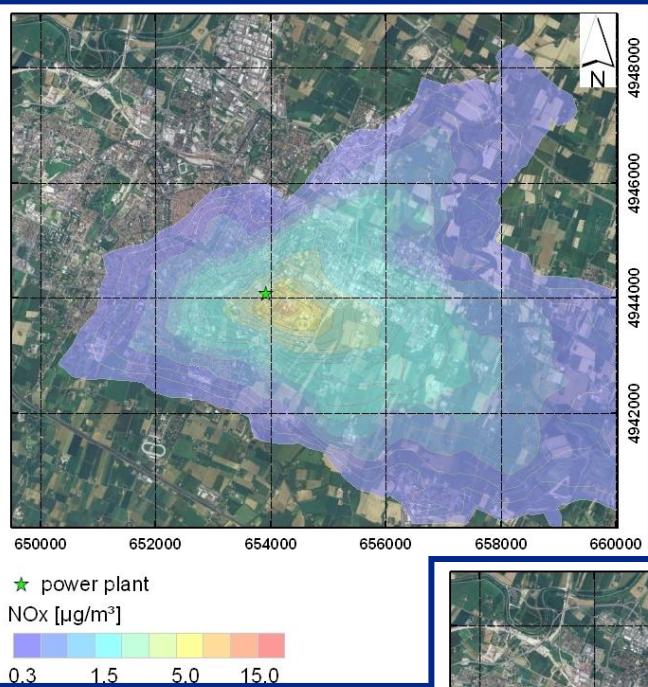
(J. D. Thomson, 1987)

$$\begin{aligned} \frac{\partial}{\partial t} P_a(z, w, t) + \frac{\partial}{\partial z} [w \cdot P_a(z, w, t)] = \\ - \frac{\partial}{\partial w} [a_w \cdot P_a(z, w, t)] + \frac{1}{2} \frac{\partial^2}{\partial w^2} [b_w^2 \cdot P_a(z, w, t)] \end{aligned}$$



3rd and 4th order moments for PDF.
(*Bi - Gaussian* or *Gram – Charlier* PDF)

Application: comparing *emission scenarios*



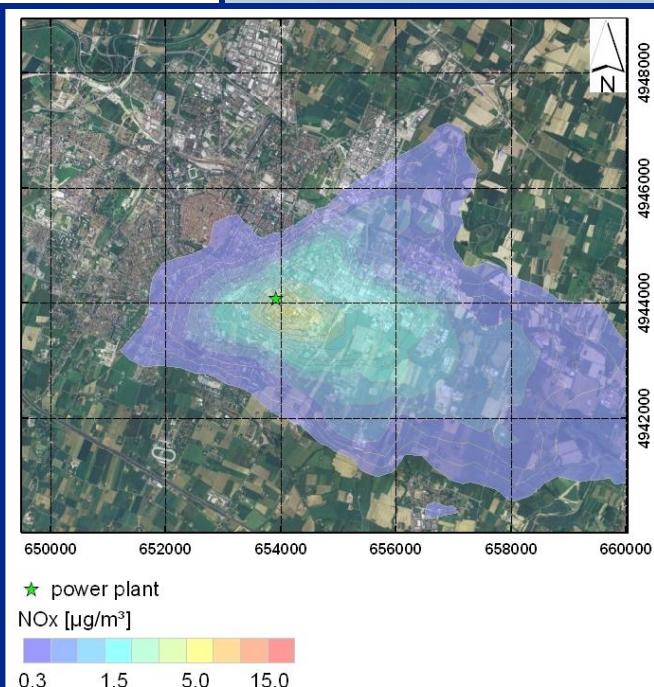
General Hospital of Modena

- **EXISTING PLANT**
conventional *boilers*
for heat production.

- **NEW PLANT**
Tri-generator
and auxiliary *boliers*.

- *Mean average concentration fields*
in *winter* season.

Environmental performances
of two plant's installations.

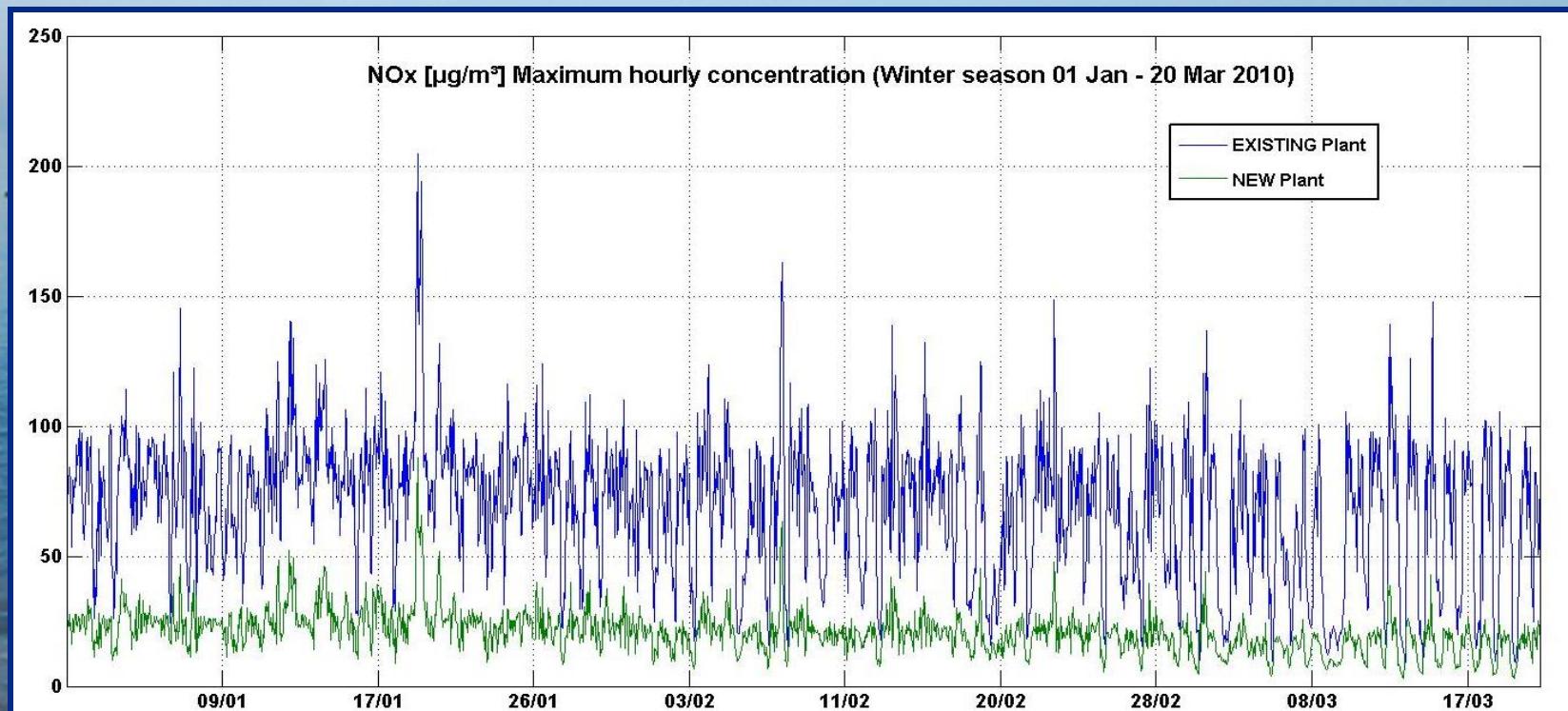


Application: compliance with *regulatory limits*

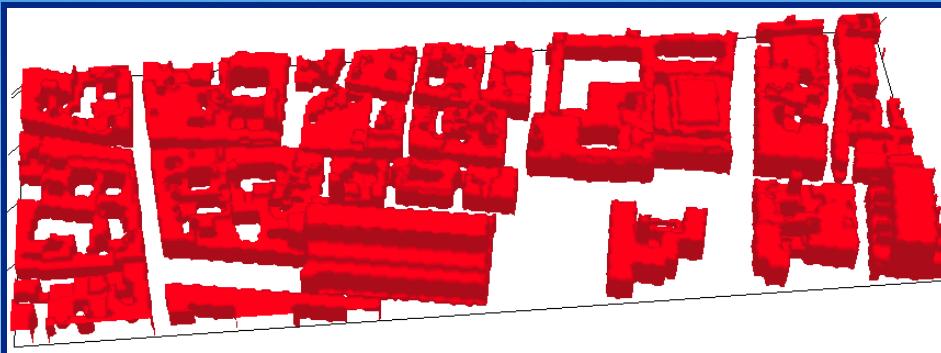
NO_x : 200 $\mu\text{g}/\text{Nm}^3$ Maximum hourly concentration (D.lgs. 155/2010)

Average of maximum NO_x hourly concentration:

- **EXISTING PLANT:** 69 $\mu\text{g}/\text{Nm}^3$ (34,5 % of the regulatory limit).
- **NEW PLANT:** 21 $\mu\text{g}/\text{Nm}^3$ (10 % of the regulatory limit).

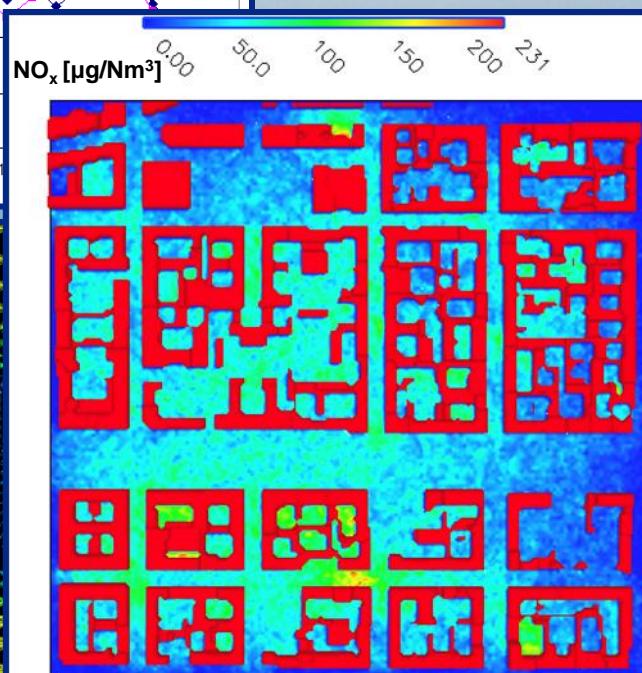
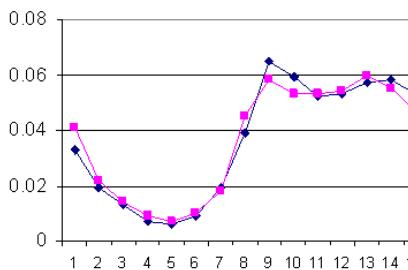


Future application: *microscale simulation*



Hourly traffic modulation

—●— transiti Ugo Bassi 2004 —■— transiti Farini 2004 (conteggi ARPA)



Microscale: 10 – 100 m.

- **Urban pollution sources**
(power or *industrial plants*, *TRAFFIC*).

• **Emission inventories**

(*Local Environmental Agencies*).

- **Urban topography:**
air flow around buildings.

- **Concentration fields:**
contribution of every source.

- **Policies and startegies:**
improving urban air quality.

References

- Tinarelli G. «*Simulazione lagrangiana a particelle della dispersione di inquinanti in atmosfera - Teoria e applicazioni*», Seminario presso la Facoltà d'Ingegneria di Modena del 17/04/2012.
- Tinarelli G. «*SPRAY 3.1 – General Description and User's guide*», Arianet R2007.08.
- Brusasca G. et al., (2007) “*Micro-Swift-Spray (MSS) a new modelling system for the simulation of dispersion at microscale. General description and validation*”, Air Pollution Modelling and its Applications XVII, C. Borrego and A.N. Norman eds., Springer, 449-458.
- Anfossi D. et al., (2000) “*A new high performance version of the Lagrangian particle dispersion model SPRAY, some case studies*”, Air Pollution Modelling and its Applications XIII, S.E. Gryning and E. Batchvarova eds., Kluwer Academic / Plenum Press, New York, pp.499-507.
- Finzi G., Pirovano G. e Volta M. (2001): “*Gestione della qualità dell'aria – Modelli di simulazione e previsione*”, McGraw-Hill.
- Sozzi R. (2003): “*La micrometeorologia e la dispersione degli inquinanti in aria*”, Centro tematico Nazionale Atmosfera Clima Emissioni.

**THANKS FOR YOUR
ATTENTION!!!**

Marco Zaccanti

... any questions?

GITISA – Summer School 2012
Tecnologie sostenibili per la tutela dell'ambiente

LAGRANGIAN PARTICLE MODELS FOR AIRBORNE POLLUTANT DISPERSION

Applications and research purposes

DIIAR
Technical School of Milan
25/06/2012

Eng. Marco M. Zaccanti
University of Modena e Reggio Emilia
marcomichele.zaccanti@unimore.it